## LINEAR ALGEBRA 1 PROBLEM SHEET 1

PROF. DANIEL SKODLERACK

**Problem 1** (10 points, Morgan's law). Prove the second Morgan's law, see Proposition 9(b). **Problem 2** (10 points, truth table). Compute the truth table for the following logical expression.  $((p \land \neg q) \Rightarrow (r \land (q \lor p))) \Rightarrow ((p \land \neg r) \lor (q \lor p))$ 

**Problem 3** (5+5 points, row echelon form). Find a row echelon form for the matrix

$$(0.1) \qquad \qquad \begin{pmatrix} 2 & 1 & 1 & 5 & 1 \\ 3 & 5 & -1 & 2 & 2 \\ 0 & 4 & 2 & 3 & 5 \\ 3 & 2 & 1 & 4 & 3 \end{pmatrix}.$$

Can you find the reduced row echelon form for (0.1)?

**Problem 4** (10 points, linear system). Is there a linear system (with real variables) with exactly two solutions? Give a proof for your answer.

*Date*: Please hand in before the lecture by **11<sup>th</sup> of October 2023**. For all exercises the results need to be proven using results from this lecture and the lectures before, provided you give a reference.